



# **Nonlinear Finite Element Analysis of Reinforced Concrete Beams Strengthened in Shear with Embedded Steel Bars**

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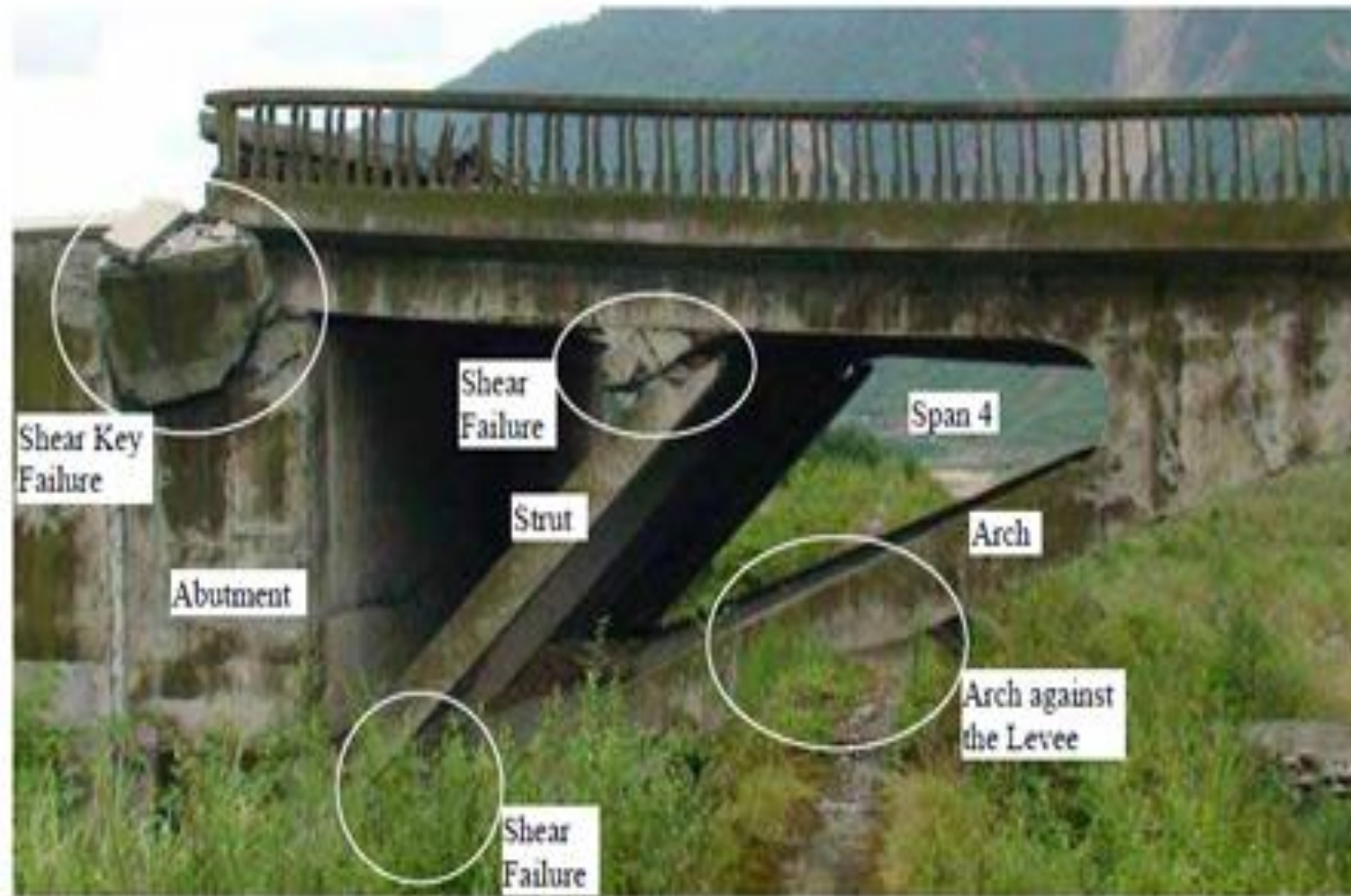
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# Content



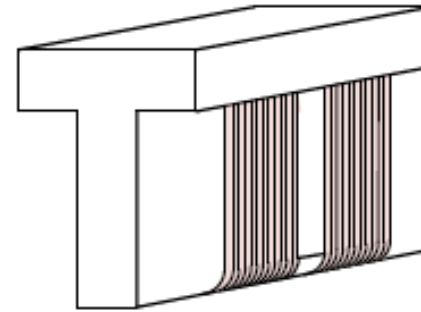
- **Background**
- **Research Questions**
- **Finite Element Modeling**
- **Results**
- **Summary**

# Background

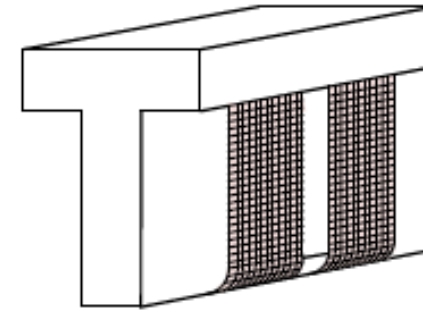


China Earthquake Reconnaissance Report: Performance of Transportation Structures During the May 12, 2008, M7.9 Wenchuan Earthquake

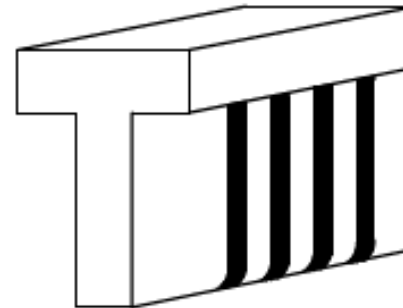
# Background: Shear Strengthening of RC beams



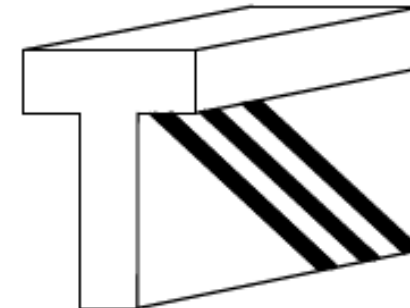
(a) EB unidirectional FRP sheets



(b) EB bi-directional FRP sheets



(c) EB laminated FRP sections

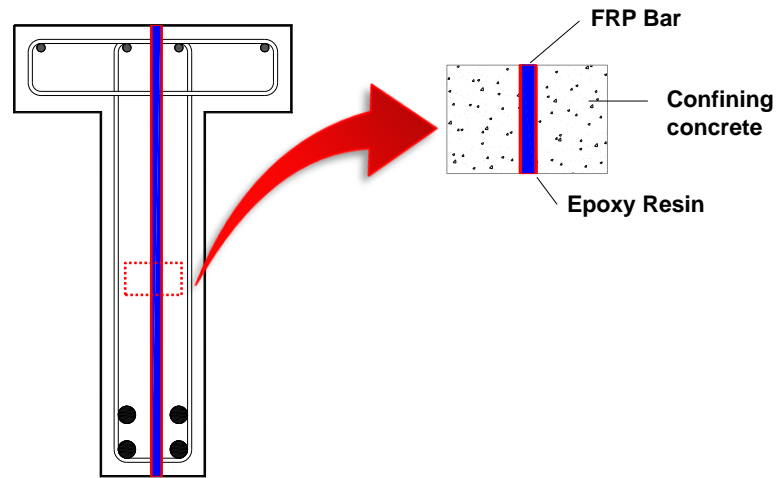


(d) NSM FRP reinforcement

Source: <https://www.horseen.com/project/strengthening-rehabilitation-rc-beam-column?page=3>

# Background

## Deep Embedment / Embedded Through-Section Technique



- ✓ Easier to apply
- ✓ Less epoxy consumption
- ✓ Higher effectiveness



# Research Questions



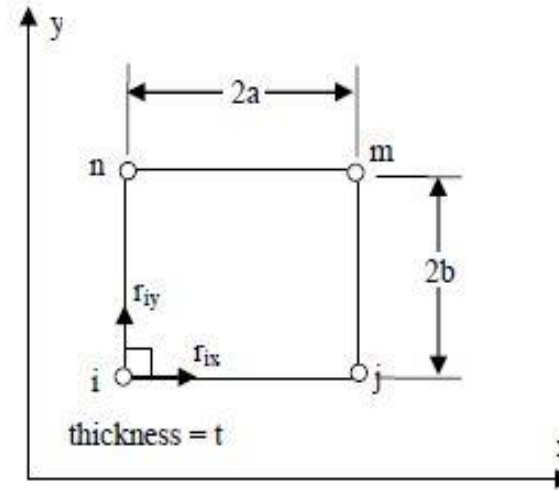
- **Shear behavior of continuous RC beams strengthened with DE/ETS technique is still unclear.**
- **The effect of concrete compressive strength on the behavior of DE/ETS strengthened continuous RC beams and simply supported RC beams is not quantified.**

# Finite Element Modeling

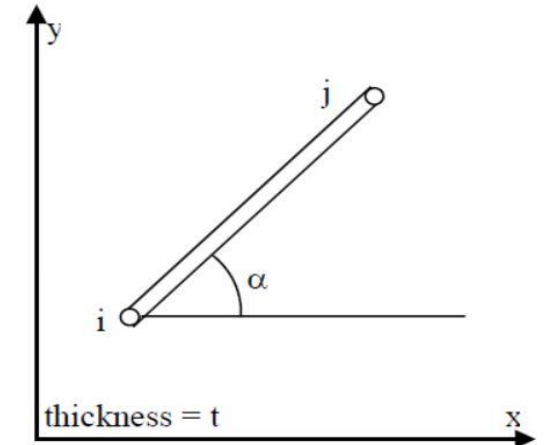


- Geometry :

- Two-dimensional, four-node, plane stress rectangular elements were used to model the concrete, loading plate and support plate.
- The steel reinforcement; comprising longitudinal reinforcement, shear links and DE/ETS bars; was modelled using two-node truss elements.



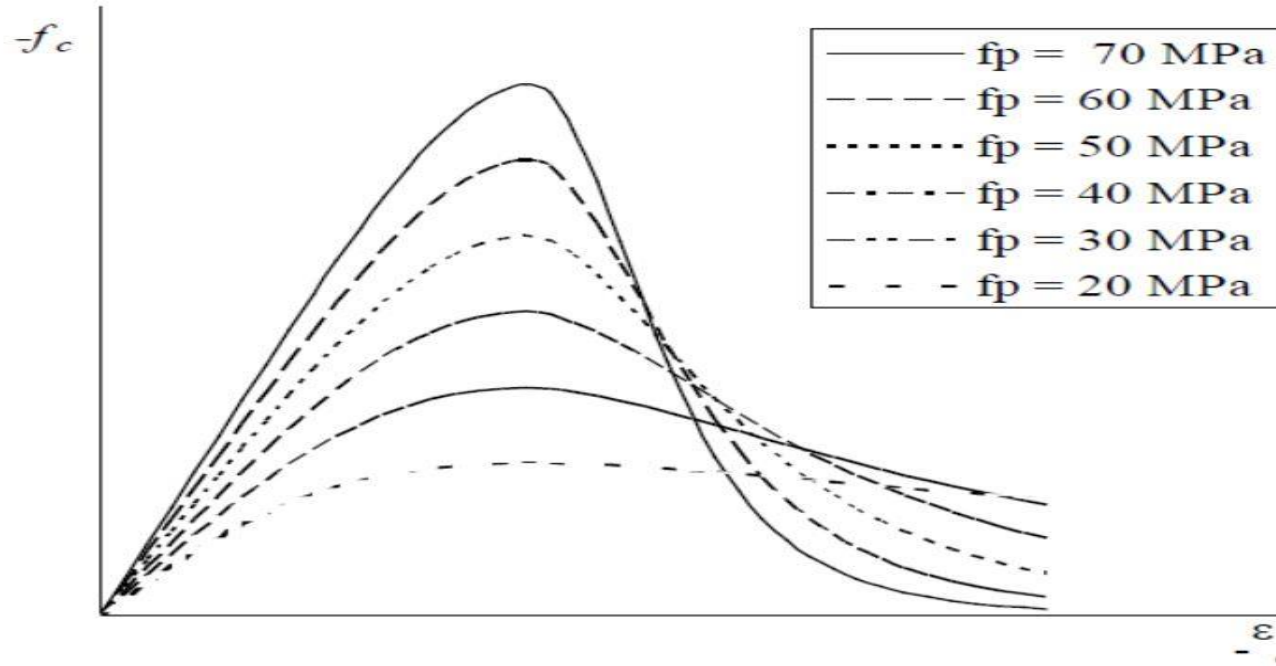
Plane Stress Rectangular Element



Truss Bar Element

# Finite Element Modeling

- Material :



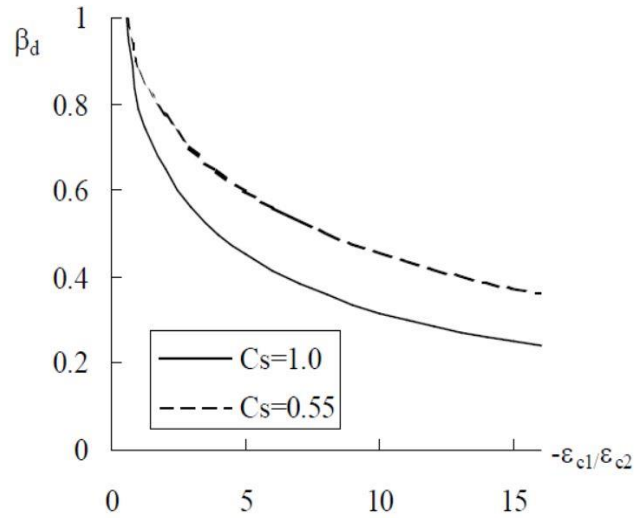
Popovics high strength pre-peak and post-peak concrete compression response



# Finite Element Modeling

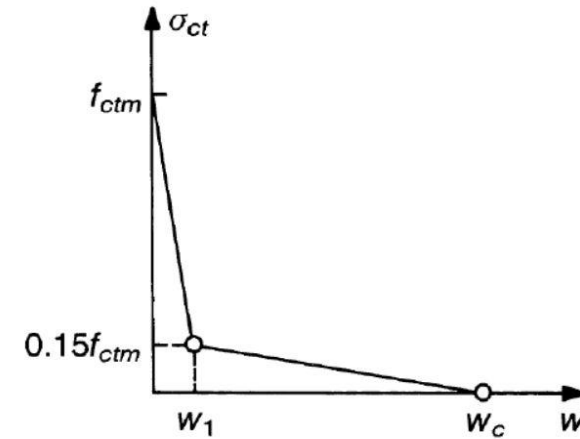


## Compression Softening



Vecchio 1992-B (e1/e0-Form) Compression softening model

## Tension Softening

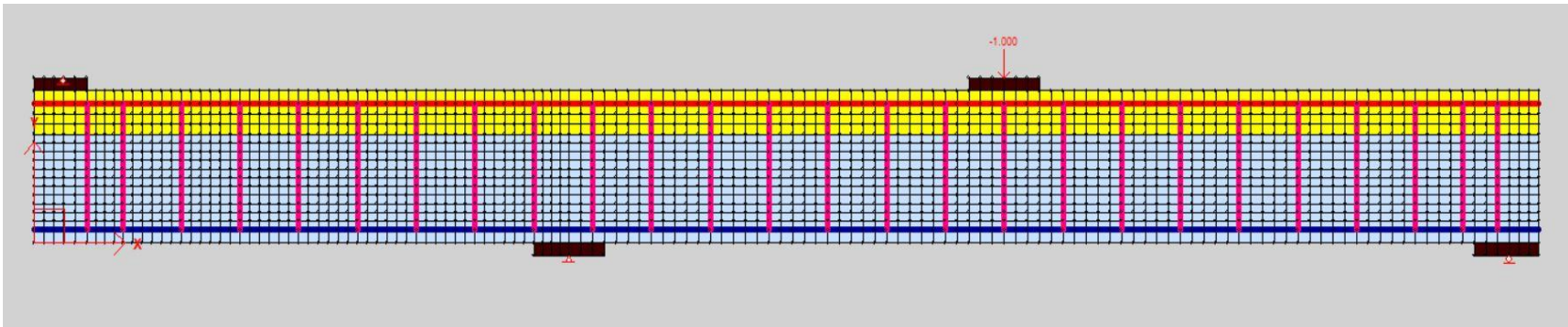


CEB-FIP tension softening curve (CEB-FIP, 1990)

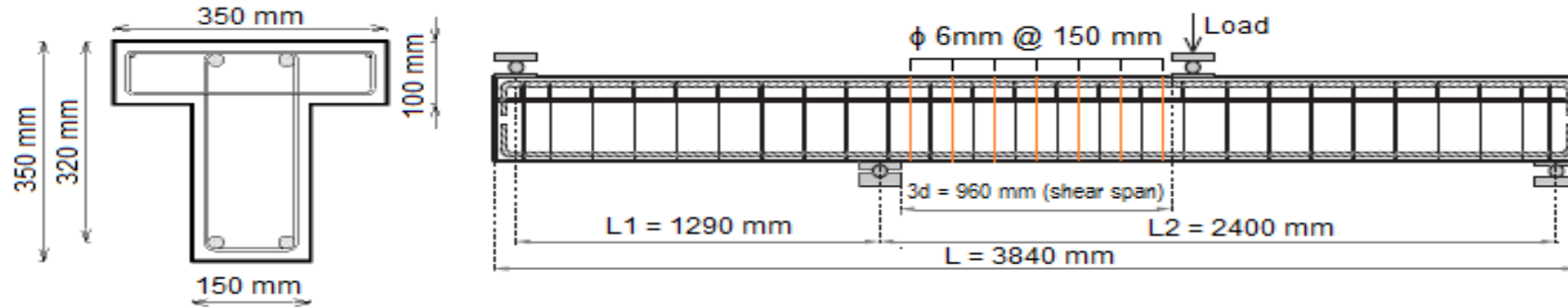
# Finite Element Modeling



Analysis Details		Material Types	
Total Number of Nodes:	6521		
Total Number of Elements:	7264		
Number of Triangular elements:	0		
Number of Rectangular Elements:	6232		
Number of Truss Elements:	1032		
Number of Linkage Elements:	0		
Number of Contact Elements:	0		
Number of Concrete Types:	3		
Number of Load Stages:	1		
Analysis Type:	VecTor2 V.4		
Analysis Parameters			
Convergence Criteria	Displacements - Weighted	Enter Job Title Struct.S2E 15th march	
Compression Base Curve	Popovics (HSC)	Displacement Factor = 0.00	
Compression Post-Peak	Popovics / Mander	1.00 2.00 3.00	
Compression Softening	Vecchio 1992-B		
Tension Stiffening	Modified Bentz 2003		
Tension Softening	Bilinear		
FRC Post-Crack Tension	SDEM (Monotonic)		
Confinement Strength	Kupfer / Richart		
Concrete Dilatation	Variable - Isotropic		
Cracking Criterion	Mohr-Coulomb (Stress)		
Crack Stress Calc	Basic (DSFMM/CFT)		
Crack Width Check	Crack Limit (10 mm)		
Concrete Bond	Perfect Bond		
Concrete Creep / Relax	Not Considered		

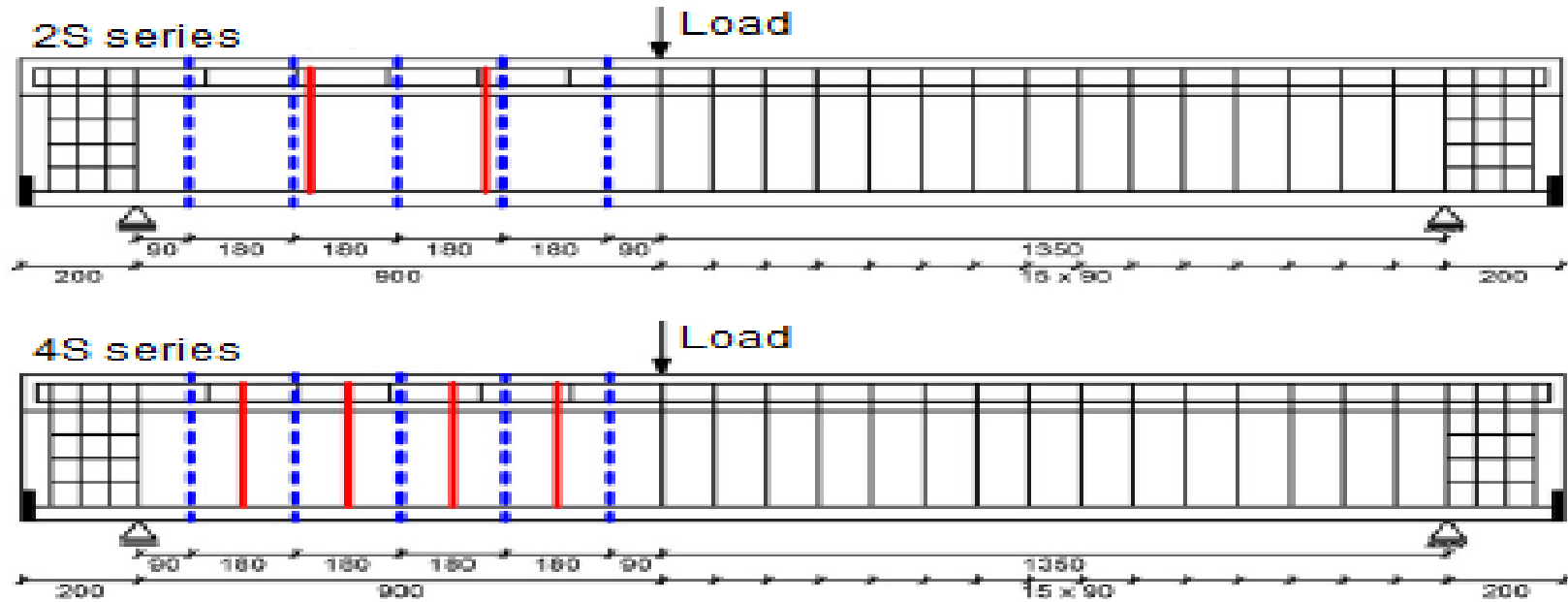
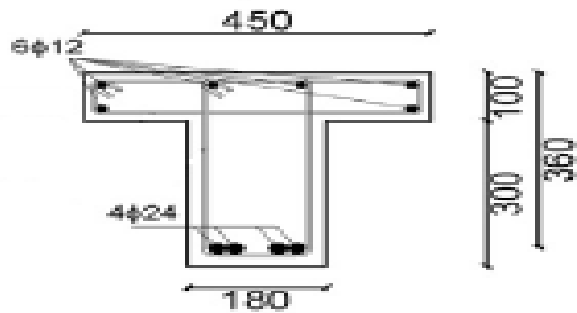


# Finite Element Modeling: Model Validation



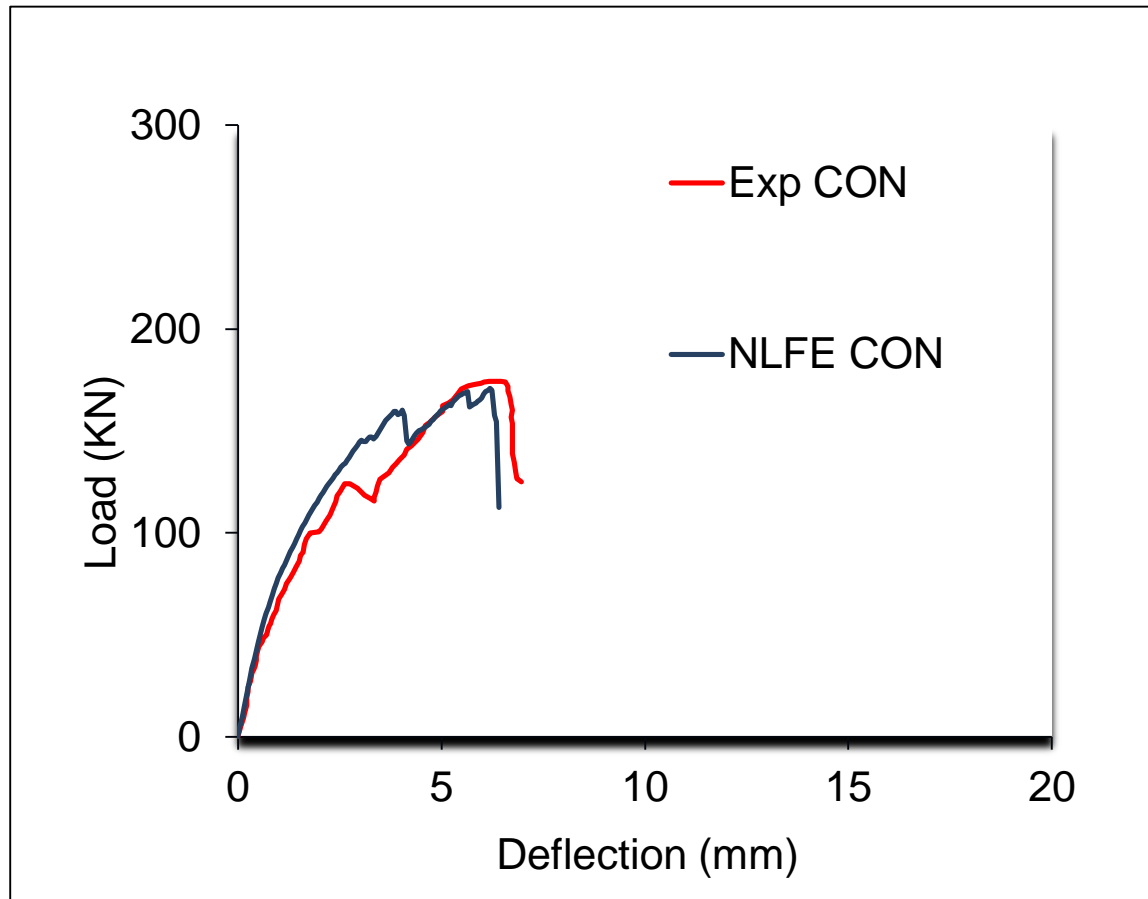
- The first set comprised the two continuous RC beams CON and S150 tested by Raicic et al. (2017)
- CON as control beam whereas S150 is strengthened with 6 mm diameter DE/ETS steel bars.
- Both beams had two 20 mm diameter tension and compression reinforcement together with 4 mm diameter shear links spaced at 150 mm.

# Finite Element Modeling: Model Validation

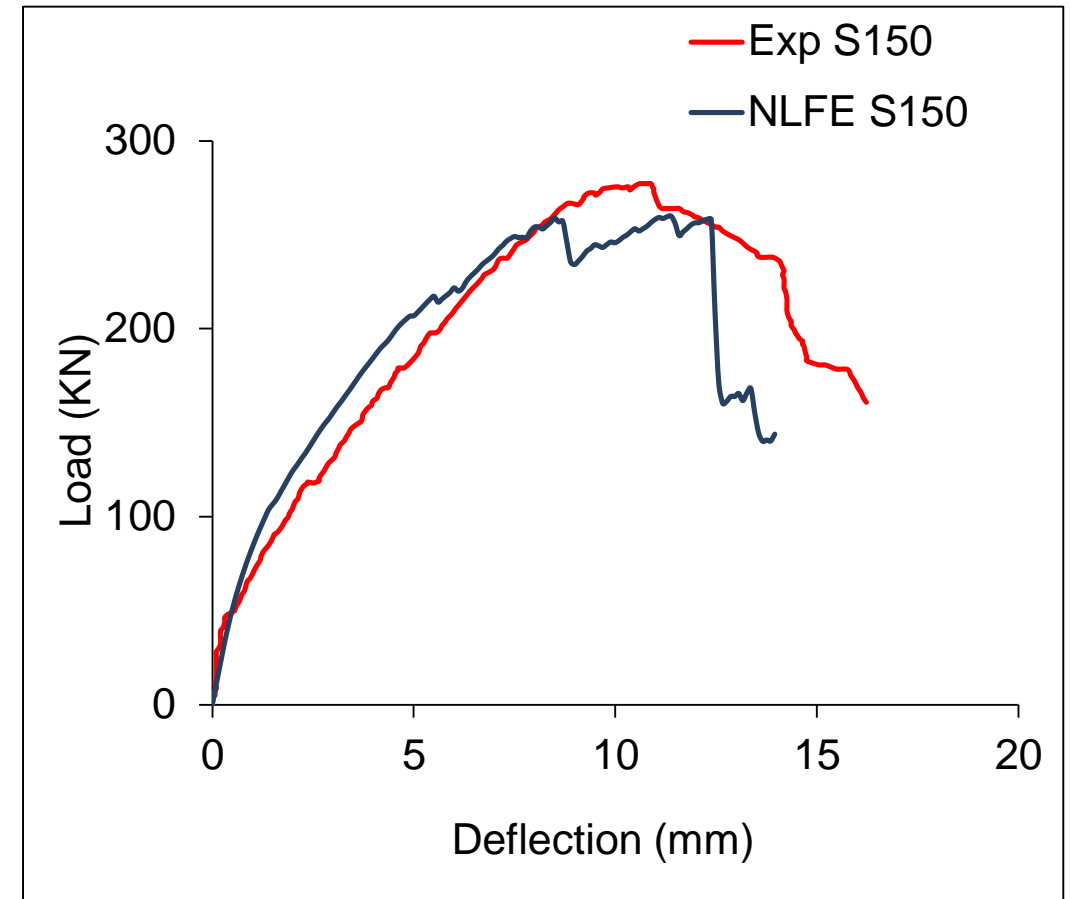


- The second set included the four simply supported RC beams 2S-Ref, 2S-S180-90, 4S-Ref and 4S-S180-90 tested by Breveglieri et al. (2015)
- The difference between the two series is that the beams in series 2S had 6 mm diameter shear links spaced at 300 mm, corresponding to a shear reinforcement ratio of 0.10% whereas the beams in series 4S had 6 mm diameter shear links spaced at 180 mm, corresponding to a shear reinforcement ratio of 0.17%.
- 2S-Ref and 4S-Ref are unstrengthened control beams whereas 2S-S180-90 and 4S-S180-90 are strengthened with 10 mm diameter DE/ETS steel bars.

# Results : Load-Deflection

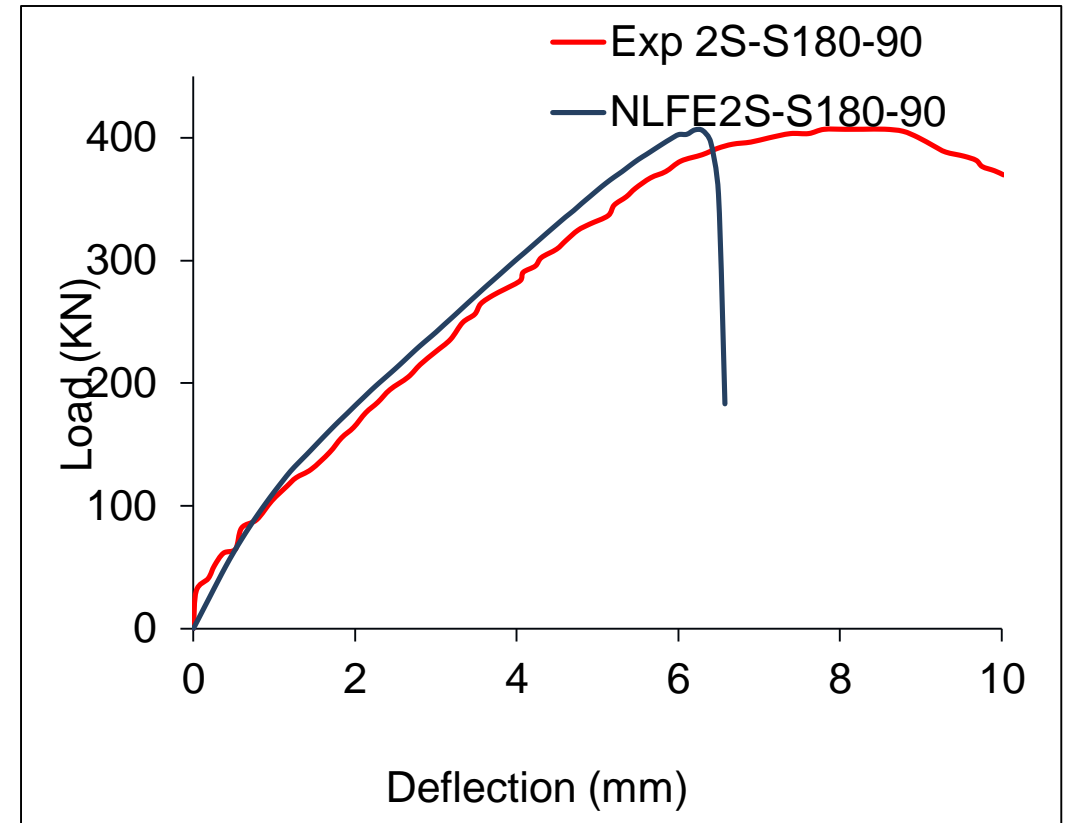
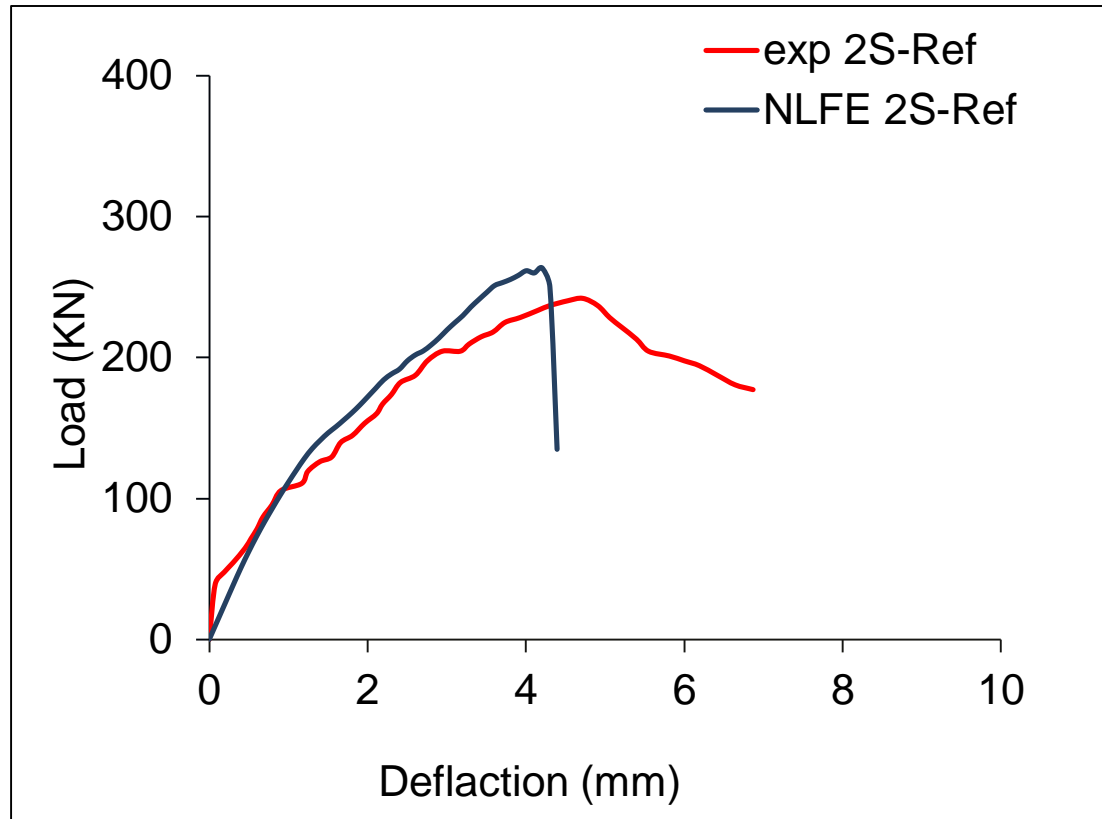


Control Continuous T Beam



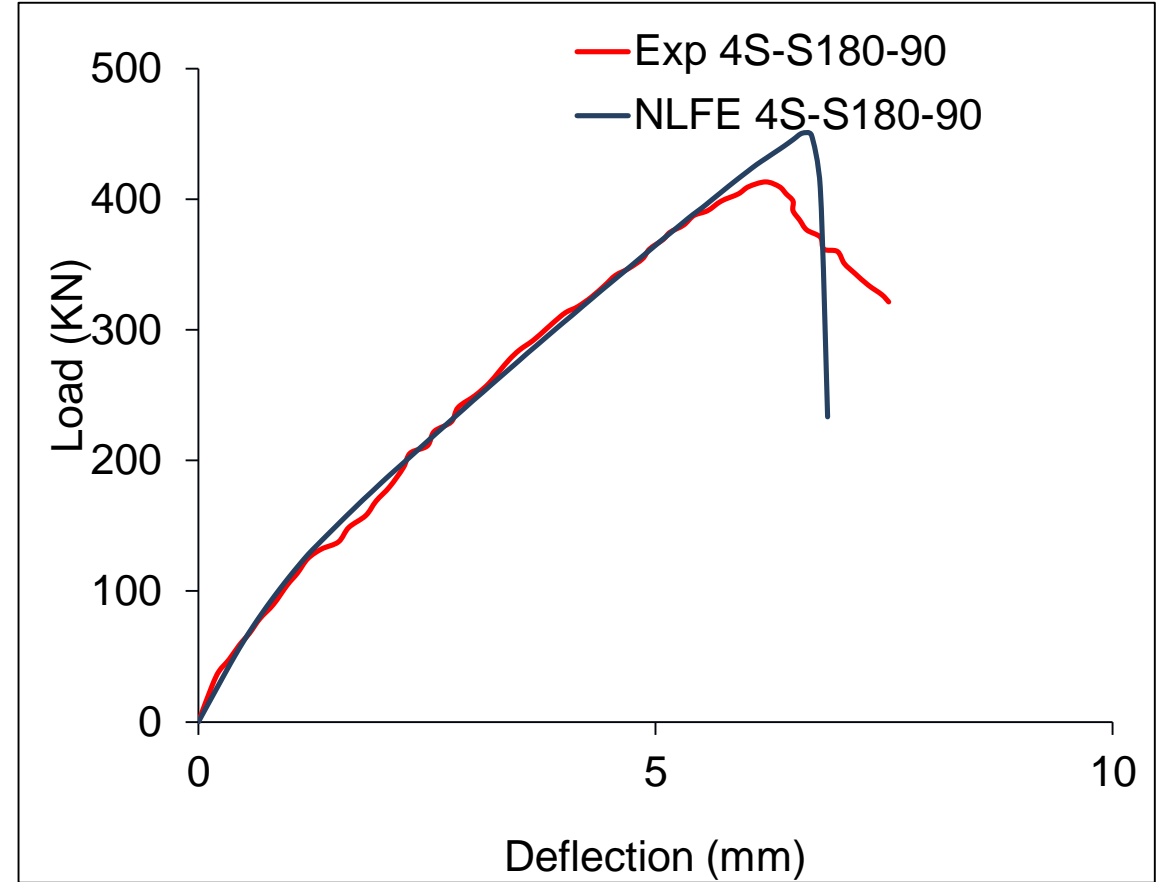
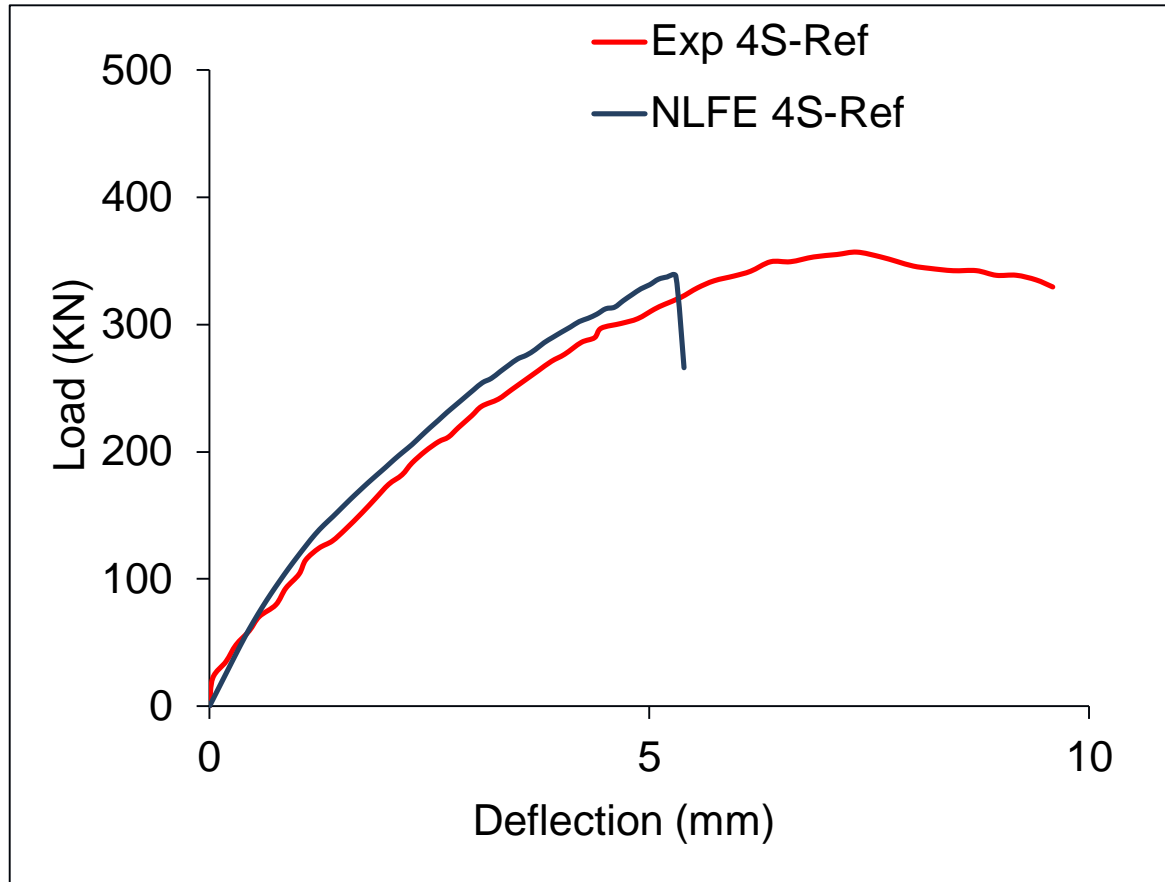
Continuous T beam Strengthened with Steel bar

# Results : Load-Deflection



Simply supported T beam ( 2S – Series )

# Results : Load-Deflection



Simply supported T beam ( 4S – Series )

# Results : Load-Deflection



Specimen	Load at Failure (KN) Experimental	Load at Failure (KN) NLFE	NLFE/Experimental	Deflection at failure load [mm] Experimental	Deflection at failure load [mm] NLFE	NLFE/Experimental
CON	173	169.32	0.98	5.7	5.637	0.98
S 150	278	258.96	0.93	10.7	8.5	0.79
2S-Ref	242.1	263.626	1.08	4.70	4.204	0.89
2S-S180-90	406.8	406.428	0.99	8.27	6.205	0.75
4S-Ref	353.8	338.036	0.95	7.35	5.301	0.72
4S-S180-90	413.2	450.569	1.09	6.32	6.607	1.04

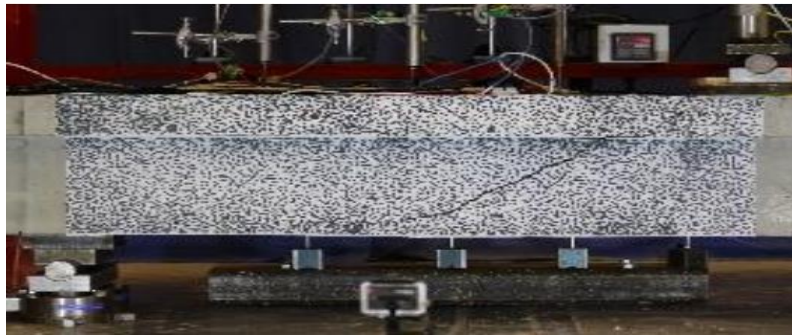
1.003 with a standard deviation of 0.061. (Load)  
 0.861 with a standard deviation of 0.118. (Deflection)



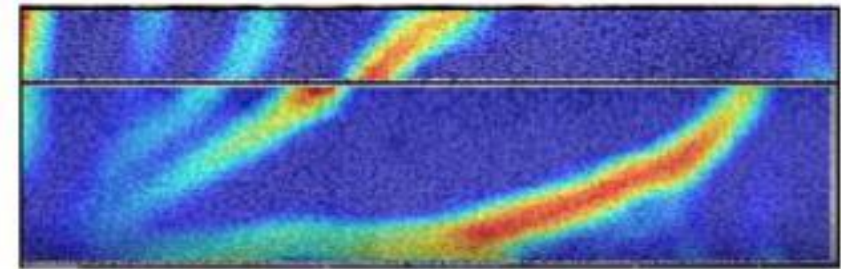
# Results : Failure Mode



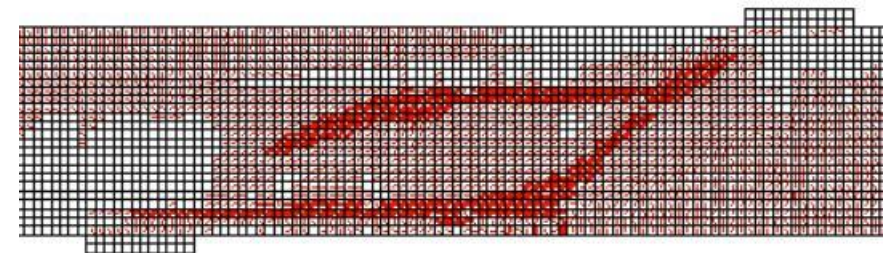
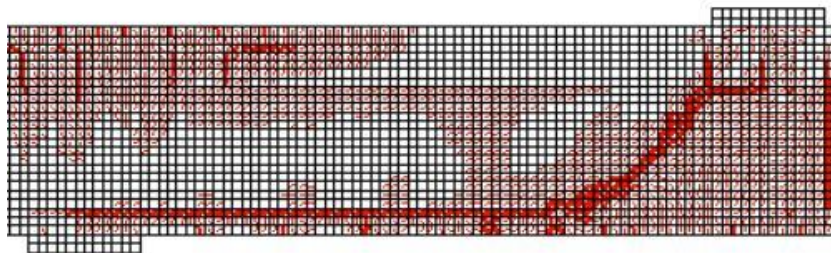
- Crack Patterns of Continuous T Beam



CON



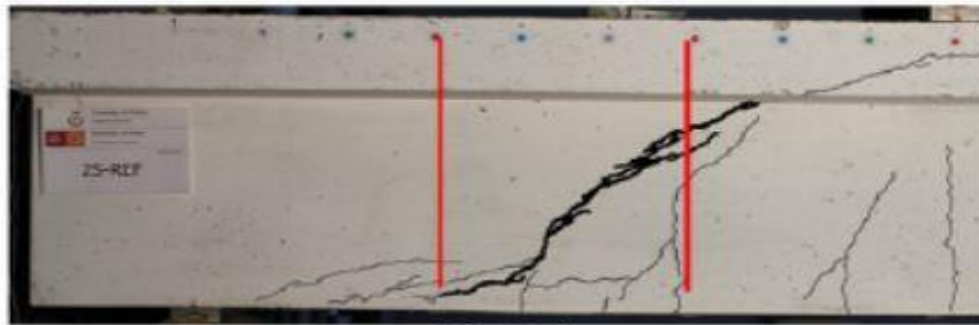
DE150



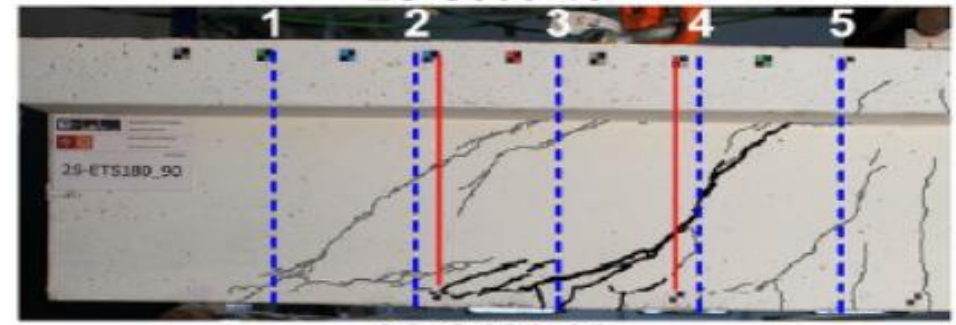
# Results : Failure Mode



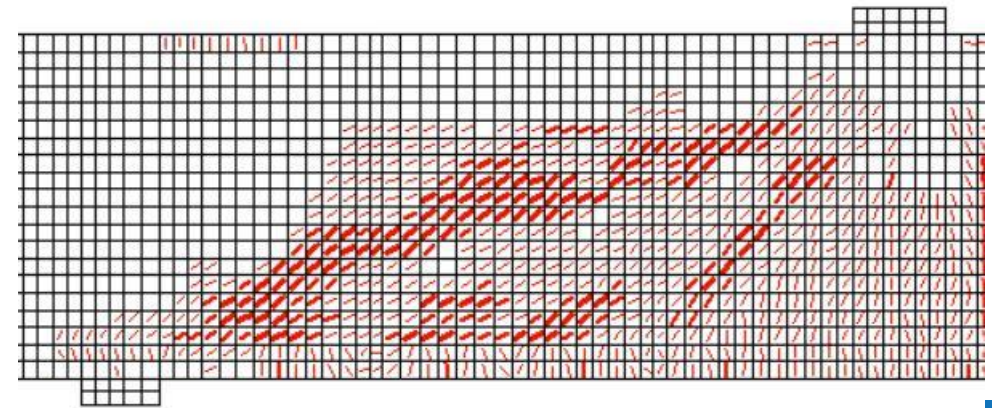
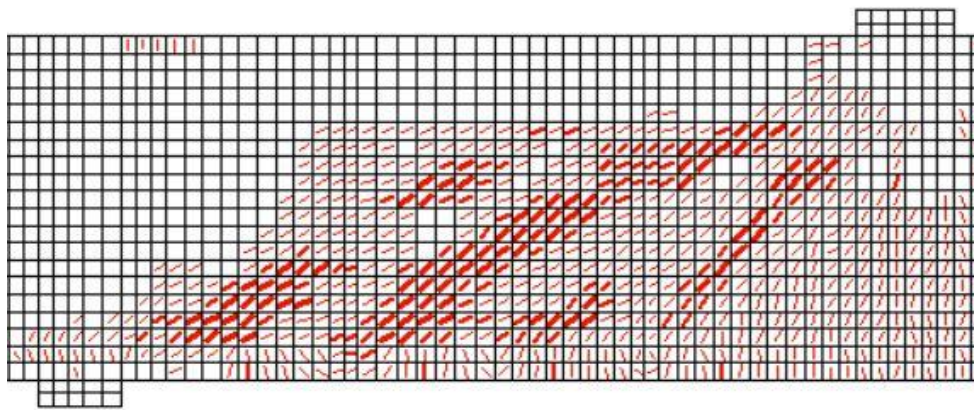
- Crack Patterns of Simply supported T Beam (2S series)



2S-Ref



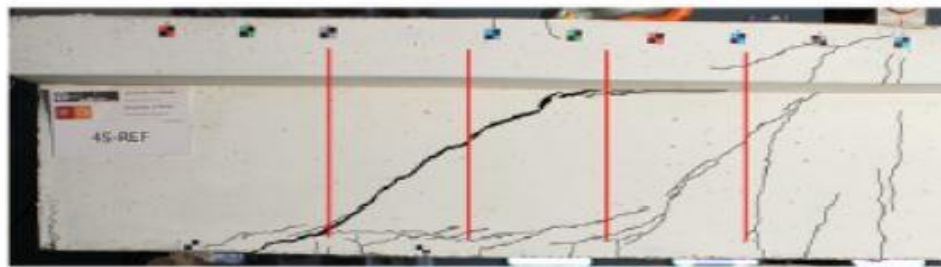
2S-S180-90



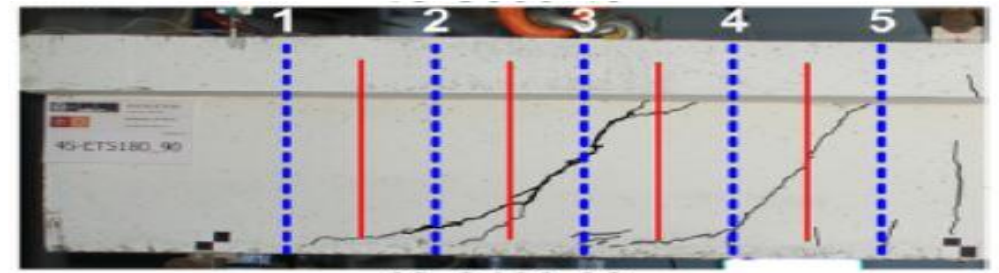
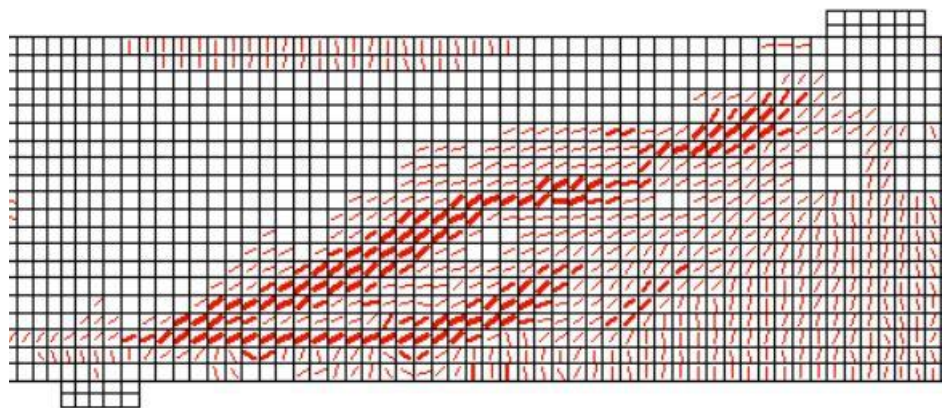
# Results : Failure Mode



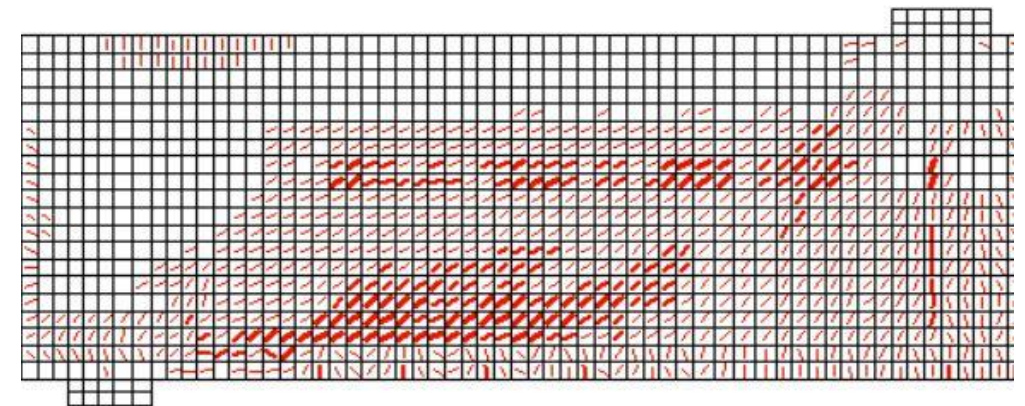
- Crack Patterns of Simply supported T Beam (4S series)



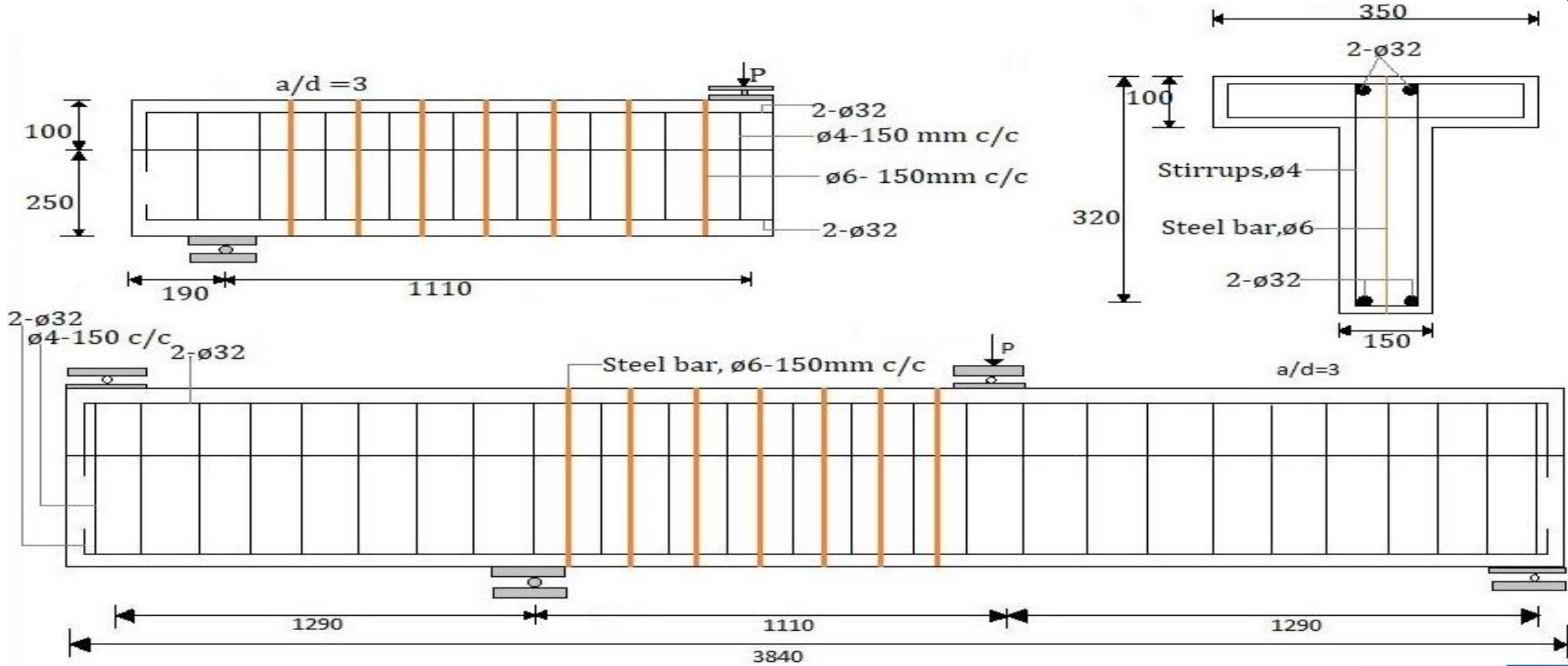
4S-Ref



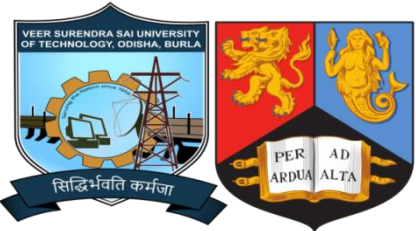
4S-S180-90



# Results: Parametric Study

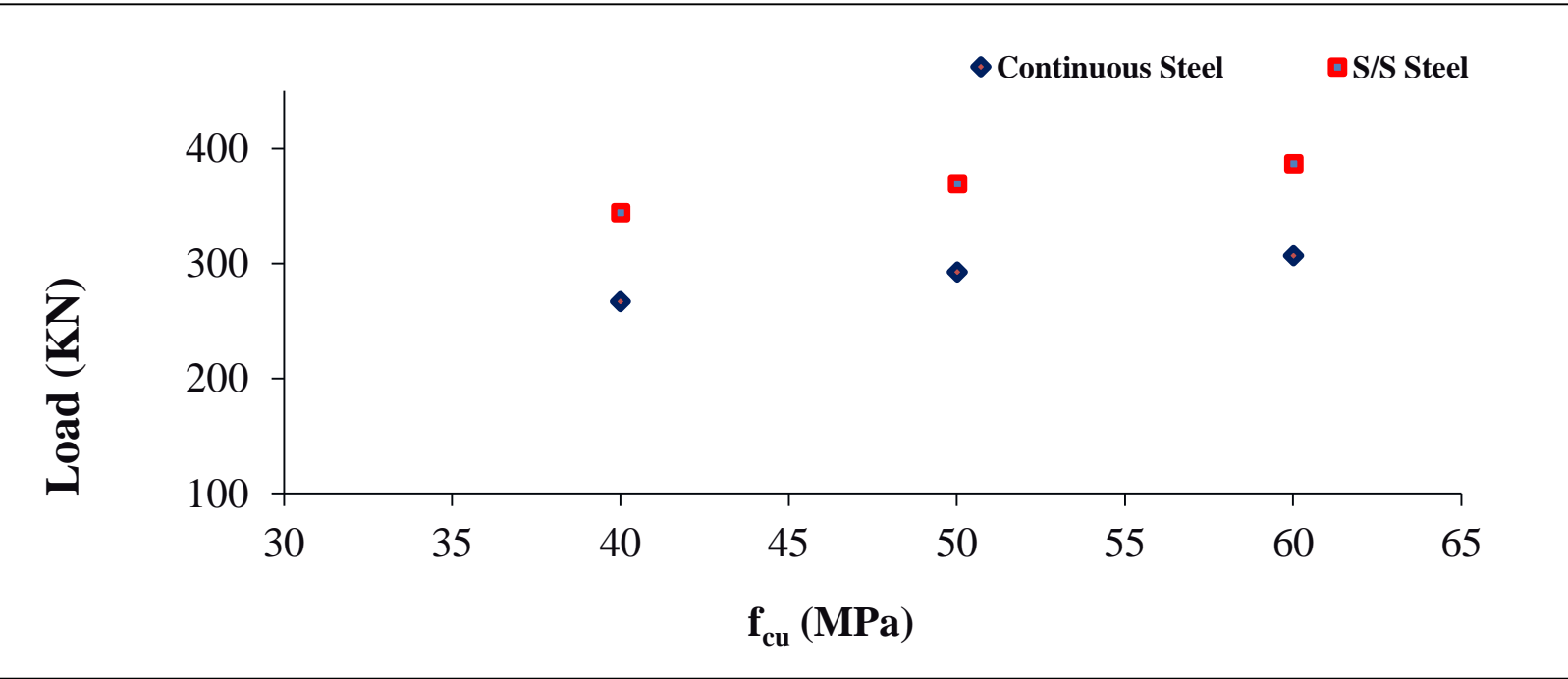


# Results: Parametric Study



- Effect of beam type and concrete compressive strength :

Concrete cube compressive strength ( $f_{cu}$ ) values of 40, 50 and 60 MPa were considered.



# Summary



- A two-dimensional nonlinear FE models for DE/ETS-strengthened simply supported and continuous RC beams were validated using experimental results from the published literature.
- A parametric study was carried out to investigate the effect of beam type and concrete compressive strength on the predicted load carrying capacity.
- The load carrying capacities of the strengthened continuous beams were 20-22% lower than those of the corresponding simply supported beams.
- The predicted load carrying capacities of both beam types increased by 12-15% with the increase in concrete cube compressive strength from 40 to 60 MPa.



# Thank You

Any questions?